A Structural Meta-Analysis of Welfare-to-Work Experiments and Their Impacts on Children

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 Setting: welfare reform experiments and their impacts on children.
- Frisch (1933) had the answer: "use a model".

Traditional meta-analysis:

- Single parameter of interest: Average Treatment Effect (α)

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- example: welfare experiment populations are highly selected and treatments are complicated bundles.

Structural meta-analysis:

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- Differences in design and setting useful for identification and well articulated inside model
- Outcomes can be calculated for full range of counterfactuals
 Todd & Wolpin (2005), Attanasio, Meghir & Santiago (2011), Duflo, Hanna & Ryan (2012), Rodriguez (2018)

Application: Welfare Reform

- Obtained micro data from three RCT evaluations of welfare-to-work programs by MDRC
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 - Time limits on participation
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- Four crucial design choices ← identification
 - Benefit formulae (generosity and work incentives)
 - Time limits on participation
 - Work requirements
 - Child care subsidies
- The model can:
 - Forecast counterfactual policy environments
 - Forecast same policy when rest of environment changes (labor markets, taxes, etc)
 - Forecast same policy on general population (experiment popn highly selected)

Model

- Environment:

- Agent is single mother, endowed with L = 112 hours per week.
- Type k, site l, treatment arm j, time t
- Investment period is $T = 17 \times 4$ quarters.
- Choices:
 - Participate in food stamps/welfare, $S \in \{0,1\}, \ A \in \{0,1\}$
 - Work, $H \in \{0,1\}$
 - If H = 1, choose formal care (F = 1) or informal care (F = 0)
 - Invest in child (1) or consume privately (C)

Value today child skills welfare status welfare remaining job offer Payoff today + work welfare childcare investment child skills +

=

 $+ \quad \beta \times Value \ tomorrow$

child skills welfare status welfare remaining job offer

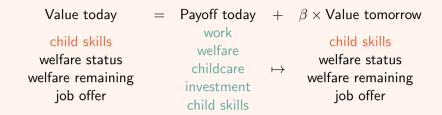
show me math

Value today	=	Payoff today	+	$\beta imes {\sf Value tomorrow}$
child skills welfare status welfare remaining job offer		work welfare childcare investment child skills	\mapsto	child skills welfare status welfare remaining job offer

Preferences:

 $u_k(C, d, A_{t-1}, \theta; \mathcal{R}) = \log(C) + \alpha_{\theta,k} \log(\theta) - \alpha_{H,k} H + \alpha_{F,k} F - \mathcal{R} A \alpha_R (1-H) - \alpha_P (1-A_{t-1}) A + \epsilon_d$

 ϵ_d is nested logit, variances $(\sigma_P, \sigma_H, \sigma_F)$, k indexes latent type.

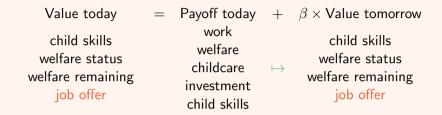


Technology:

$$\theta_{t+1} = I_t^{\delta_{l,t}} \theta_t^{\delta_{\theta}}, \qquad \kappa = H + F$$

- Let $g_{\kappa,t}I_t$ be solution to cost-minimization problem, $\kappa \in \{0,1,2\}$

- Will estimate prices $(g_{0,t}, g_{1,t}, g_{2,t})$



Earnings:

$$\log(W_{klt}) = \mu_k + \beta_{W,1} \text{Unemp}_{lt} + \beta_{W,2} \text{Age} + \eta_t$$

where η_t follows a job ladder process with separation rate δ_k , and job offer rates $\lambda_{0,k}, \lambda_{1,k}$.

Work requirements can improve job-finding: $\lambda_{0,k}^{\mathcal{R}} > \lambda_{0,k}$.

Value today	=	Payoff today	+	$\beta imes Value$ tomorrow
child skills welfare status <mark>welfare remaining</mark> job offer		work welfare childcare investment child skills	\mapsto	child skills welfare status welfare remaining job offer

Resource constraint:

 $C + g_{\kappa}I + p_{F,klj}F \leq Y_{ljt}(S, A, H \times W_{klt}) + y_k$

Identification of Production

Model yields outcome equation:

$$\log(\theta_t) = \mu_k + \sum_{s=0}^t \delta_{\theta}^{t-s} \left(\delta_l \log(\text{net income}_s) + \tilde{g}_1 \times \text{Mom Working}_s \right)$$
$$+ \tilde{g}_2 \times \text{Formal Care Used}_s + \delta_{\theta}^t \log(\theta_0) + \xi_t$$

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$$+ \tilde{g}_2 \times \text{Formal Care Used}_s + \delta_{\theta}^t \log(\theta_0) + \xi_t$$

Which implies two sets of moment conditions:

- 1. Use assignment to treatment conditional on location.
- 2. Use all variation conditional on a flexible function of type and η_0 .

other parameters

Estimation

Strategy:

- Use SIPP to pin down distribution of latent variables in representative population.
- Estimate initial distribution of latent variables directly.
- Stage 1: Estimate prices, transitions, preferences, via maximum likelihood.
- Stage 2: Bayesian estimation of production parameters using pseudo-likelihood implied by each of two moment conditions.

Estimation - Data

	CTJF	CTJF	FTP	FTP	MFIP	MFIP	MFIP	SIPP
Arm	0	1	0	1	0	1	2	0
Less than Highschool	0.401	0.428	0.437	0.476	0.346	0.353	0.368	0.273
Highschool	0.495	0.481	0.533	0.502	0.443	0.453	0.456	0.351
Some College	0.093	0.078	0.025	0.02	0.211	0.194	0.176	0.299
College	0.012	0.012	0.004	0.002	0	0	0	0.078
AFDC Participation	0.51	0.498	0.39	0.354	0.464	0.571	0.643	0.253
Foodstamps Participation	0.606	0.614	0.552	0.546	0.488	0.115	0.14	0.337
Mother's age	26.691	26.767	27.039	26.752	26.268	26.462	26.683	28.2
Number of Children	1.807	1.809	1.99	1.96	1.688	1.724	1.817	1.754
Employed	0.497	0.556	0.446	0.479	0.486	0.539	0.485	0.639
Earnings	534.185	551.806	337.862	376.537	538.512	560.03	461.347	1550.693
Person-Quarter Observations	35939	37255	28035	27972	52614	47214	31482	11197
Individuals	1956	2025	1335	1332	2923	2623	1749	953

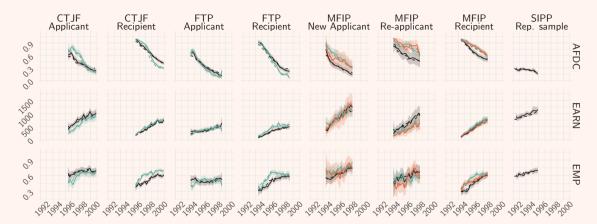
Preference Estimates

	Type-Specific Parameters						
Туре	α_H	α_{A}	α_{S}	α_F	$lpha_{ heta}$	у	
k=1	-0.63	-0.34	-0.66	0.18	0.32	229.71	
	(0.12)	(0.03)	(0.07)	(0.22)	(0.00)	(38.63)	
k = 2	-1.01	-0.46	0.21	0.85	0.28	627.79	
	(0.15)	(0.03)	(0.02)	(0.28)	(0.00)	(69.32)	
k = 3	-0.97	-1.14	0.95	1.17	0.23	1105.14	
	(0.15)	(0.08)	(0.08)	(0.34)	(0.00)	(122.96)	
k = 4	0.10	-1.04	1.05	-0.99	0.18	147.67	
	(0.19)	(0.08)	(0.09)	(0.12)	(0.00)	(22.71)	
k = 5	-1.07	-1.82	1.73	0.20	0.17	1979.23	
	(0.20)	(0.16)	(0.16)	(0.16)	(0.00)	(308.73)	
		Global Parameters					
	β	σ_3	σ_2	σ_1	α_R	α_P	
	0.34	1.16	0.56	0.34	0.04	1.63	
	(0.05)	(0.24)	(0.04)	(0.03)	(0.02)	(0.15)	

Wage Process

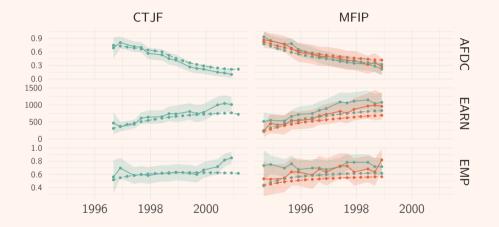
	Type-Specific Parameters						
Туре	λ_0	λ_1	δ				
k = 1	0.15	0.53	0.11				
	(0.00)	(0.03)	(0.00)				
k = 2	0.19	0.74	0.10				
	(0.01)	(0.04)	(0.00)				
k = 3	0.16	0.48	0.27				
	(0.00)	(0.03)	(0.01)				
k = 4	0.06	0.66	0.02				
	(0.00)	(0.03)	(0.00)				
k = 5	0.08	0.24	0.05				
	(0.00)	(0.02)	(0.00)				
	Global Parameters						
	μ_o	σ_o	λ_R				
	-0.43	0.88	0.42				
	(0.02)	(0.02)	(0.04)				

Model Fit



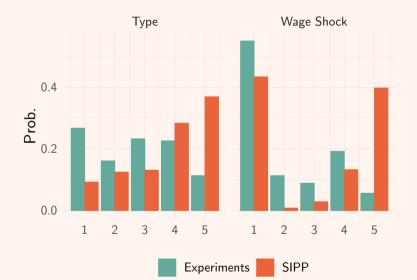
Arm — 0 — 1 — 2 — Data --- Model

Validation: Holdout Sample



Arm - 1 - 2 Data --- Model

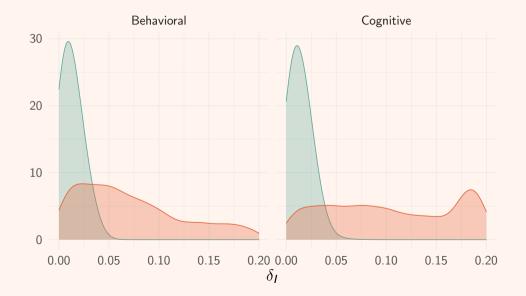
Evidence of Strong Selection in Experiments



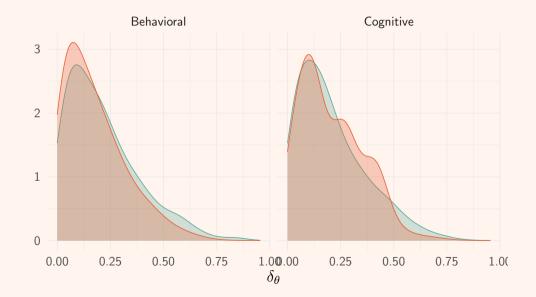
Factor Loadings

Measure	λ_B^m	λ_B^m	σ_m^2
BPI-Externalizing	-3.70	-	5.86
	(0.14)		(1.23)
BPI-Internalizing	-2.32	-	7.55
	(0.08)		(0.91)
Positive Behavior Scale	6.49	-	63.34
	(0.23)		(23.84)
School Engagement	0.16	0.96	2.03
	(0.14)	(0.14)	(0.10)
Ever Repeat Grade	0.79	-0.80	0.04
	(0.25)	(0.25)	(0.00)
Ever Suspended	-0.05	-0.05	0.08
	(0.02)	(0.02)	(0.00)
School Achievement - Parent	-	0.51	0.72
		(0.03)	(0.02)
School Achievement - Teacher	-	0.42	1.29
		(0.06)	(0.09)

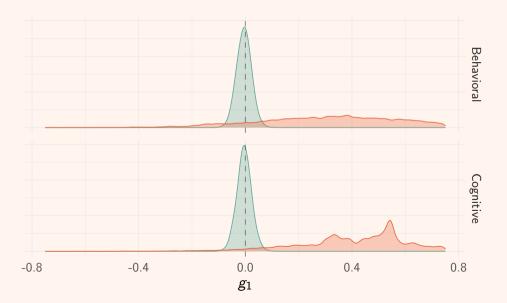
Estimates of the return to resources (δ_I)



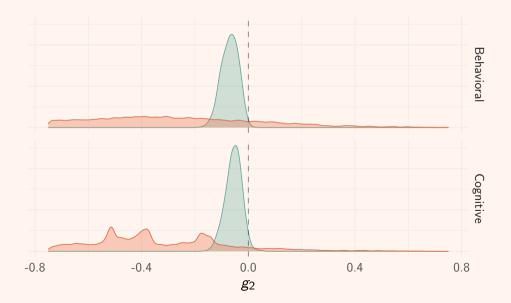
Effects show rapid decay



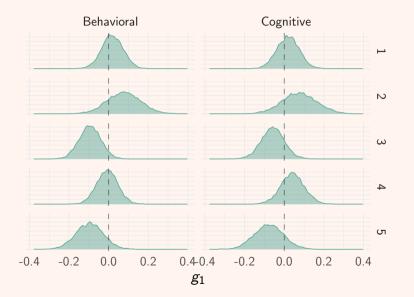
IV doesn't tell us much about effects of care



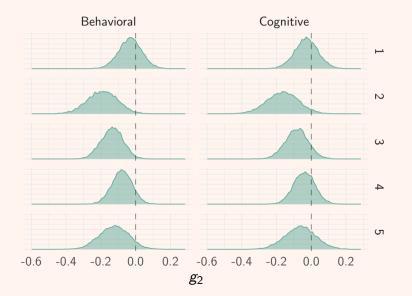
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Care effects are heterogeneous

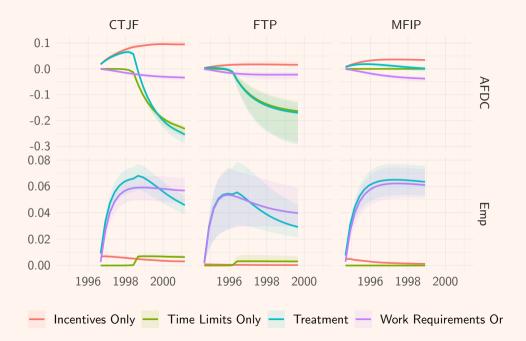


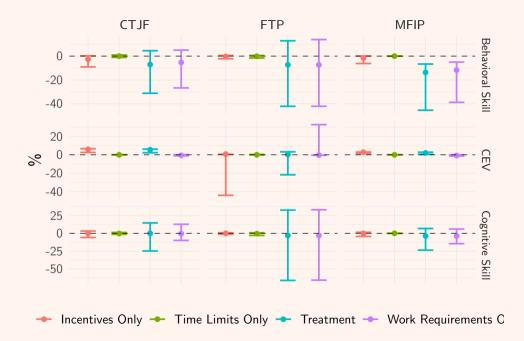
Care effects are heterogeneous



- What components of the treatment were responsible for the treatment effects?
- What would outcomes look like if we used only one reform instead of an ensemble?
- What would the impacts on children be?

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- What would outcomes look like if we used only one reform instead of an ensemble?
- What would the impacts on children be?
- We can explore this using the model by introducing each piece in isolation.





No Negative Impacts on Skills in Experiment Population

	FTP				
	Treatment	Incentives Only	Work Requirements Only	Time Limits Only	
Behavioral Skill	-7.27	-0.29	-7.33	-0.10	
	[-18.95, 16.09]	[-1.74, 0.30]	[-18.99, 16.19]	[-0.99, 0.88]	
Cognitive Skill	-3.05	0.01	-2.91	-0.38	
	[-14.19, 15.37]	[-0.51, 1.33]	[-14.10, 15.58]	[-1.56, 0.50]	
CEV	0.37	0.67	-0.32	-0.00	
	[-18.98, 5.06]	[-31.05, 0.50]	[-0.72, 21.99]	[-0.01, 0.13]	
		CTJF			
	Treatment	Incentives Only	Work Requirements Only	Time Limits Only	
Behavioral Skill	-7.02	-2.72	-5.26	-0.00	
	[-22.80, 1.96]	[-7.08, 0.15]	[-18.04, 2.31]	[-0.84, 0.74]	
Cognitive Skill	0.02	0.28	-0.37	-0.20	
	[-9.62, 10.33]	[-3.61, 3.74]	[-9.33, 8.54]	[-1.14, 0.70]	
CEV	5.49	5.97	-0.59	-0.00	
	[3.16, 6.25]	[3.46, 6.36]	[-1.44, 0.44]	[-0.02, -0.00]	

Changing the Population of Interest

- What would the effects of these policies be on the general population, not just on applicants?
- What would the effect on child outcomes be?
- We can use the model to explore this, applying these policies to the SIPP sample.

Negative Impacts on Skills in Broader Population

Table: Treatment Effects

	FTP	CTJF	MFIP
Behavioral Skill	-10.00	-12.10	-12.25
	[-36.32, -3.09]	[-44.14, -3.94]	[-43.65, -4.52]
Cognitive Skill	-2.84	-4.03	-3.65
	[-12.38, 5.16]	[-14.97, 5.94]	[-14.20, 5.82]
CEV	1.19	2.80	2.03
	[0.83, 1.53]	[2.36, 3.19]	[1.60, 2.42]

Conclusion

- In some contexts, the effects of many experiments or quasi-random policy interventions are well understood through standard economic models
- Other potential examples: job training, microfinance, minimum wages.
- This is one context in which the model appears to work quite well.
- Researchers must still make decisions about what variation they are willing to use.
- Model uncovers rich treatment effect heterogeneity with implications for broad effect of policies

- Type selection for each site *I*:

```
P[k|I, X_m] \propto \exp(X_{m,I}\beta_{I,k})
```

where X_m includes number of kids, age of youngest kid, education, and application status.

- Then estimate $P(\eta|k, \mathsf{App \ status})$ nonparametrically.
- Impose that η is drawn from stationary distribution in SIPP.

go back

Parameter

What it determines (show me math)

Preferences

Var of participation util. shocks (σ_P)

Response of participation to program generosity

Parameter

Preferences

Var of participation util. shocks (σ_P)

Var of work util. shocks (σ_H)

What it determines show me math

Response of participation to program generosity Response of work to financial incentives

Parameter

Preferences

Var of participation util. shocks (σ_P) Var of work util. shocks (σ_H)

Var of formal care util. shocks (σ_F)

What it determines show me math

Response of participation to program generosity Response of work to financial incentives Response of child care use to price changes

Parameter

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Var of participation util. shocks (σ_P) Var of work util. shocks (σ_H)

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Utility costs of work requirement $(\alpha_{R,k})$

What it determines (show me math)

Response of participation to program generosity Response of work to financial incentives Response of child care use to price changes Effect of work requirements on work while participating.

Parameter

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Var of participation util. shocks (σ_P)

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Utility costs of work requirement $(\alpha_{R,k})$

Technology

Log-relative price of investment (\hat{g}_1, \hat{g}_2)

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Effect on child outcomes of non-maternal care

Parameter

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Utility costs of work requirement $(\alpha_{R,k})$

Technology

Log-relative price of investment (\hat{g}_1, \hat{g}_2) Cobb-Douglas share on investment (δ_l) What it determines (show me math)

Response of participation to program generosity Response of work to financial incentives Response of child care use to price changes Effect of work requirements on work while participating.

Effect on child outcomes of non-maternal care

Effect on child outcomes of increase in income

Parameter

Preferences

Var of participation util. shocks (σ_P)

Var of work util. shocks (σ_H)

Var of formal care util. shocks (σ_F)

Utility costs of work requirement $(\alpha_{R,k})$

Technology

Log-relative price of investment (\hat{g}_1, \hat{g}_2) Cobb-Douglas share on investment (δ_l) Cobb-Douglas share on skills (δ_{θ}) What it determines show me math

Response of participation to program generosity Response of work to financial incentives Response of child care use to price changes Effect of work requirements on work while participating.

Effect on child outcomes of non-maternal care Effect on child outcomes of increase in income Persistence of effects on child outcomes

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- With choice probabilities and finite dependence, identification guaranteed by conditional moments of random assignment only.

Model - Full

Dynamic program:

$$V_{kjt}(\theta_t, \omega_t) = \mathbb{E} \max_{l_t, d_t} \left\{ u_k(C_t, d, \theta_t; \mathcal{R}_{kj}) + \epsilon_d + \beta V_{kjt+1}(\theta_{t+1}, \omega_{t+1}) \right\}$$

Subject to:

$$U(C, d, \theta) = \alpha_C \log(C) + \alpha_\theta \log(\theta) - \alpha_{H,k}H - \alpha_{A,k}A + \alpha_{F,k}F + \epsilon_d$$
$$\theta_{t+1} = I_t^{\delta_{l,t}} \theta_t^{\delta_{\theta}}, \qquad I_t = \mathcal{I}_t(\tau, x, H, F)$$
$$C + x + p_{F,kj}F + w_q(\tau + 30H) \le Y_{kjt}(A, H) + w_qL$$

too much math!!!

Model - Specifying Technology

- Work with dual:

$$e(I, H, F) = \min_{\tau, x} w_q \tau + x$$
 s.t. $\mathcal{I}_t(\tau, x, H, F) \ge I$

- Linear expenditure function:

$$e(I,H,F) = g_{\kappa,t}I_t, \qquad \kappa = H + F \in \{0,1,2\}$$

- Marschak (1953): sufficient to estimate prices $(g_{0,t}, g_{1,t}, g_{2,t})$, subject to policy invariance.
- Note interpretation of prices

Model - Budgets (Control Group Example)

$$Y_{k0t}(A, H) = E_{kt}H + A \cdot [AFDC_{kt}(E_{kt}H) + SNAP_t(E_tH)]$$

AFDC_{kt}(E) = max{B_k(n, y) - (1 - 0.33) max{E - 120, 0}, 0}

- $B_k(n, y)$ is benefit standard for family size n in year y
- Fixed earnings disregard of \$120/month
- Variable earnings disregard of 33% of monthly earnings
- Treatments will modify these parameters, affecting incentives.

Model - Work Requirements and Time Limits

- Let \mathcal{R}_{kj} indicate whether a work requirement applies:

 $u_k(C, d, \theta; \mathcal{R}) = \alpha_C \log(C) + \alpha_\theta \log(\theta) - \alpha_{H,k}H + \alpha_{F,k}F - \mathcal{R}A[\alpha_{R,k}(1-H)] + \epsilon_d$

- Let Ω be the number of periods of welfare use permitted. For control groups, $\Omega=\infty.$
- Let ω track the number of periods remaining:

$$\omega_{t+1} = \omega_t - A_t$$

- When $\omega = 0$, eligible for food stamps only.

MDRC's Welfare to Work Experiments

- 5 experiments, welfare recipients randomly assigned:
 - Family Transition Program, Minnesota Family Investment Program, National Evaluation of Welfare-to-work Strategies, Jobs First, LA Greater Avenues for Independence
 - 1991-1999
- Data compiled from publicly available reports

Bloom, Kemple, Morris, Scrivener, Verma, and Hendra (2000), Bloom, Scrivener, Michalopoulos, Morris, Hendra, Adams-Ciardullo, Walter (2002), Freedman, Knab, Gennetian, and Navarro (2000), Gennetian and Miller (2000), Hamilton, Freedman, Gennetian, Michalopoulos, Walter, Adams-Ciardullo, and Gassman-Pines (2001), Miller, Knox, Gennetian, Dodoo, Hunter, and Redcross (2000) Some other things you should know about these experiments:

- Treatment randomly assigned to applicants (both new and those for re-certification)
- Slightly more complicated for NEWWS and LA-GAIN (part of assignment to existing JOBS program).
- <u>No significant impacts</u> on hours, wages, fertility. Minimal impact on marital status.

go back

Let Δ denote the difference operator between treatment *j* and control outcomes:

$$\mathbb{E}\Delta\log(\theta_{t+1}) = \delta_{l,t} \Big(\sum_{D} \Delta P_{kjt,D} \big[\log(Y_{k0t}(H,A) + w_q(L-30H)) - \hat{g}_{\kappa,t} \big] \\ P_{kjt,D}\Delta\log(Y_{kt}(H,A)) \Big) + \delta_{\theta} \mathbb{E}\Delta\log(\theta_t)$$

where $\hat{g}_{\kappa,t} = \log(g_{\kappa,t}/g_{0,t})$ is the relative log-price under formal and informal care. too much mathill

Identification of Preferences I

Let $\rho_{kjt}(\omega) = P[A = 1|k, j, t, \omega]$. When no time limit applies:

$$\log\left(\frac{\rho_{kjt}(\infty))}{1-\rho_{kjt}(\infty))}\right) = \alpha_{\mathcal{C},t} \log\left(\frac{Y_{kjt}(0,1) + w_q L}{w_q L}\right) - \sigma_H \log\left(\frac{1-P_{H,t}(1)}{1-P_{H,t}(0)}\right) - \mathcal{R}_{kj} \alpha_{R,k} - \alpha_{H,k}$$

And under time limits:

$$\log\left(\frac{\rho_{kjt}(\omega)}{1-\rho_{kjt}(\omega)}\right) - \log\left(\frac{\rho_{kjt}(\infty)}{1-\rho_{kjt}(\infty)}\right) = \beta \left[\log\left(\frac{\rho_{kjt+1}(\omega)}{1-\rho_{kjt+1}(\omega-1)}\right) - \log\left(\frac{\rho_{kjt+1}(\infty)}{1-\rho_{kjt+1}(\infty)}\right)\right]$$

Parameters identified by levels and treatment responses.

Identification of Preferences II

Fixing the choice of A, formal care use:

$$\log\left(\frac{P_{F,kjt}(A)}{1 - P_{F,kjt}(A)}\right) = \sigma_F^{-1} \left[\alpha_{C,t} \log\left(\frac{Y_{kjt}(1,A) + w_q(L-30) - p_{F,k}}{Y_{kjt}(1,A) + w_q(L-30)}\right) + \alpha_{F,k} - \Gamma_t(\hat{g}_{2,t} - \hat{g}_{1,t}) \right]$$

Work:

$$\log\left(\frac{P_{H,kjt}(A)}{1 - P_{H,kjt}(A)}\right) = \sigma_{H}^{-1} \left[\alpha_{C,t} \log\left(\frac{Y_{kjt}(1,A) + w_{q}(L-30) - p_{F,k}}{Y_{kjt}(0,A) + w_{q}L}\right) - \alpha_{H,k} + A\mathcal{R}_{kj}(\alpha_{R,k} - \alpha_{R2,k}) + \alpha_{F,k} - \Gamma_{t}(\hat{g}_{2,t} - \hat{g}_{1,t}) - \sigma_{F} \log(P_{F,kjt}(A)) \right]$$

Parameters identified by levels and treatment responses.